

KTH – ROYAL INSTITUTE OF TECHNOLOGY School of Computer Science and Communication

DD143X Degree Project in Computer Science, First Level

Constructing an Evaluation Function for Playing Backgammon

Authors: Anders Sjöqvist ante@kth.se

André Stenlund andreste@kth.se Supervisor: Johan Boye

14 June 2011

Abstract

In this project we describe a few variations of the game backgammon. We explain different algorithms, used to play backgammon and other similar games, and develop our own rule engine and a set of players. By developing an evaluation function for playing board games, we aim to find out if it's possible to construct a simple computerized player that outperforms other players, and which properties such a player should have. The player programs that we have developed are very primitive, but there are distinct tendencies revealing which players dominate the others. The winning player's only strategy is to hit the opponent's lone checkers, while protecting its own.

Sammanfattning

I denna uppsats beskriver vi några varianter av spelet backgammon. Vi går igenom olika algoritmer som används för att spela backgammon och andra liknande spel, och utvecklar vår egen regelmotor och en uppsättning spelare. Vi vill skapa en evalueringsfunktion för att spela brädspel så att vi ska kunna ta reda på om det går att konstruera en enkel datorspelare som vinner över andra spelare, och vilka egenskaper en sådan spelare ska ha. Spelarprogrammen som vi utvecklat är mycket primitiva, men det är ändå tydligt vilka spelare som tenderar att dominiera andra. Den vinnande spelaren har som sin enda strategi att slå ut motståndarens ensamma pjäser, medan den skyddar sina egna.

Contents

1	Introduction	3
	1.1 Statement of collaboration	3
2	Problem statement	4
3	Playing backgammon	4
	3.1 Terminology and basic rules	4
	3.2 Rules of classic backgammon	4
	3.3 Rules of Greek backgammon	
	3.3.1 Portes	
	3.3.2 Fevga	
	3.3.3 Plakoto	6
4	Computer algorithms	6
	4.1 Minimax	
	4.2 Expectimax	
	4.3 Alpha-beta pruning	
	4.4 *-Minimax	8
	4.5 Knowledge-based evaluation	8
	4.6 Neural networks	
5	Constructing our own evaluation function	9
	5.1 Research process	9
	5.2 Choice of game rules	
	5.3 Choice of algorithm	10
	5.4 Rule engine	10
	5.5 AI players	11
	5.6 Automated test framework	
6	Results	13
7	Conclusions	14
8	Further research	14
9	Acknowledgements	15
Re	eferences	15

1 Introduction

Artificial intelligence for computerized gameplay has been studied for a long time, but not until recently has the topic gained publicity. [6, p. xix] While some of the algorithms have few applications outside the domain of human-imitating gameplaying opponents, they still have quite a few things to teach us. Firstly, in their algorithmic forms they can improve our understanding of probability, tactics and consequences of previous decision-making. Secondly, they serve as measurements of the development in the computer industry, as they are one the easiest comprehensible ways of comparing human intelligence with computational thoroughness (especially in the well-known matches between computers and human world champions). Thirdly, the benefits of the development of efficient gaming opponents shouldn't be underestimated, as they provide recreation as well as sharpening of our logical and tactical abilities, which is often benefitial in other situations in our lives.

The game of *backgammon* is particularly interesting, and is one of the most studied problems. [7] It's a two-player zero-sum game with a chance element. Since we might experience "bad luck" with the dice throws, the chance element makes it impossible to develop a strategy that is guaranteed to perform well in at least 50 % of the games *in the short run*, as even a novice player can beat a skilled one thanks to luck (but note that this won't happen in the long run, when "the luck runs out"). Development of new software for playing backgammon can improve the availability of games for different platforms, as well as promote further research of the topic. Backgammon is also theoretically interesting; if we decide that the problem we want to solve is to find the true probability of winning from a given game state when both players are rational, it turns out that we don't know whether the problem is in *P*. [3] That makes it unlikely that we will find a simple algorithm for solving it anytime soon, and requires us to create methods for optimizing our guesses.

In this project, we intend to present a few different games played on the the same backgammon board and explain our reasons for choosing a certain set of rules. Furthermore, we will introduce algorithms, frequently used when implementing backgammon artificial intelligence (AI) players. Lastly, we'll describe our own experiments for constructing an evaluation function, the conclusions we drew and discuss possibilities for future research.

1.1 Statement of collaboration

This thesis has been written entirely by Anders Sjöqvist and André Stenlund. It's our firm belief that every task must be assigned to exactly one individual, or else it might be overlooked. According to this principle, André was assigned the main responsibility of coding the rule engine and gameplaying software, as well as running the tests. Anders, on the other hand, was responsible for finding appropriate literature, deciding about algorithms and writing the report. The division of responsibilities also roughly represents how the work was divided, although we made sure that we both agreed on everything. In addition, some tasks were done jointly, as exemplified by the separate rule engine written by Anders and parts of the literature search which was made by André.

2 Problem statement

We want to use Alpha-beta pruning and Expectimax to find an efficient backgammon AI evaluation function, in order to increase our own understanding, summarize some important algorithms and draw conclusions about the behavior of a few simple tactics. Preferably, these conclusions should be able to help game developers or enable future research. Specifically, this is the question we want to answer:

"Is it possible to construct an evaluation function that, using simple and humanly comprehensible rules, with statistical significance can outperform other evaluation functions in backgammon?"

3 Playing backgammon

The information in this section is available from various sources, but we recommend using Backgammon Galore for reference. [1] They also have some information about how backgammon programs work.

We will hereby explain the rules of a few games. The rules are provided for completeness, to ensure that a reader who has already played backgammon understands the rules in the same way that we do. It's out of the scope of this thesis to try to teach a beginner how to play, and although the rules that we have implemented are also described here, they might be explained more intuitively elsewhere.

3.1 Terminology and basic rules

Backgammon is a two-player game, and the game pieces (often divided into black and white) are called *checkers*. A player initiates his turn by throwing the two dice, which must be thrown together and display an unambiguous result (i.e. if at least one die lands on the floor or stops in a tilted position, both dice must be thrown again). The checkers are then, if possible, moved around the board and placed on some of the 24 points. The points are located on both sides of the board, with 12 on each side, and divided into groups of six by the vertical bar. If a point is occupied by a single checker, it's called a blot. Depending on the variant of the game, the blot might be *hit* by the opponent and placed on the bar. The six final points along the path of movement for one of the players is called that player's home board. If a player has a checker on the bar, he must enter it into the opposing home board before he can make any other move. If there are no possibilities to enter the checker, given the numbers on the dice, the player must wait a turn. Once all the checkers are gathered in the own home board, the player may start bearing off the checkers.

3.2 Rules of classic backgammon

Figure 1 depicts the initial board setup in classic backgammon. The game is played with two dice, indicating the movement of the checkers. A dice throw of {3,5} means that two checkers may be moved 3 and 5 points, respectively, or that one checker may be moved twice, a total of 8 points (but only in case a temporary stop on the 3rd or 5th point is legal, which is the case when at most one of the opponent's checkers is placed there). If both dice show the same number, the player should instead make four moves, if possible. As long as there's at least one possible move, the player is forced to move. If there are different possibilities, any is permitted.

In the setup in Figure 1, Black moves counterclockwise along increasing numbers from the

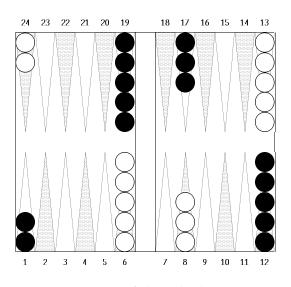


Figure 1: Setup of classic backgammon

lower left corner to the upper left. The movement of White is mirrored – from the upper left to the lower left. The objective of the game is to move all the checkers to the home board, so that they can be borne off. The first player to bear off all the checkers wins the game.

The strategy of the game is to build so-called *doors*, a point with at least two checkers. Blots are to be avoided if possible, as they can be hit by the opponent and placed on the bar. In other words, the doors both protect the checkers and prevent the opponent from landing on that point. A player may continue to move after a hit if there are any moves left, in accordance with the numbers on the dice. If there are checkers on the bar, they must be entered into the game before any other moves are allowed for that player. They are entered by landing on a free point (or a point with a blot) in the opponent's home board, according to the numbers on the dice.

Classic backgammon involes a doubling die, allowing a player, about to roll, to propose that they double the stakes. This forces the opponent to choose between continuing with raised stakes or ending the game and thereby losing the number of points that the doubling die is currently displaying.

3.3 Rules of Greek backgammon

There are, of course, other variants of backgammon than the classic one. We were also considering the three Greek games of Portes ($\Pi \delta \rho \tau \epsilon \varsigma$), Plakoto ($\Pi \lambda \alpha \varkappa \omega \tau \delta$) and Fevga ($\Phi \epsilon \upsilon \gamma \alpha$).

One difference from Western backgammon that made us consider the Greek games, was that they lack the doubling die, present in classic backgammon. Instead, if a player manages to bear off all the checkers before the opponent has borne off a single one, the winning score will be 2 instead of 1. The choice of game will be discussed and explained in subsection 5.2 and suggestions concerning inclusion of other games are mentioned in section 8. The other difference in Greek backgammon is that the winner of the opening roll rerolls for his first turn.

3.3.1 Portes

Apart from the above-mentioned differences, the game is the same as Western backgammon. The initial setup is the same as the classic, shown in Figure 1, and the name itself, Portes, refers to the strategy of building doors.

3.3.2 Fevga

Fevga means escape, and has to do with the fact that the players chase each other in the same counter-clockwise direction on the board. This setup, shown in Figure 2, is symmetrical along the diagonal rather than the horizontal.

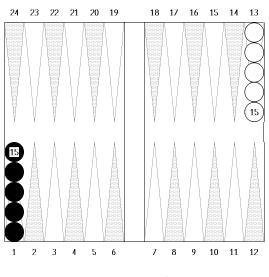


Figure 2: Setup of Fevga

There's no hitting, which means that a single checker controls a point. The strategy is to block as many points as possible, preferably in a line, to prevent the opponent from moving. Six consecutive blocked points are called a *prime*. A player is not allowed to build a prime in the starting table. They are allowed elsewhere on the board, but the player must move if all of the opponent's checkers are placed on the point immediately behind the prime.

Before being allowed to move anything else, a player must move the first checker past the starting point of the other player.

3.3.3 Plakoto

As in Fevga, there's no hitting. Instead, a blot is trapped if the opponent lands on it (even if it's with a single checker) and can't be moved until the trapping checker is moved. The closer to the starting point you get trapped the worse. The strategy is that, once having trapped important checker, place as many checkers as possible on that point, to lower the risk of having to leave the point because of unfortunate dice throws. The starting point is called the *mother*, and having the mother checker (the last remaining checker on the mother point) trapped normally means losing the game with a score of 2 (since it won't be released until the opponent bears off the last checkers), unless the opponent's mother checker is also trapped.

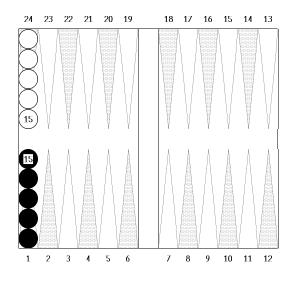


Figure 3: Setup of Plakoto

4 Computer algorithms

Backgammon is a *stochastic zero-sum* game with *perfect information*. Given that one player wins as much as the other player loses, the game is zero-sum. [6, p. 73][8] Unlike Poker, there's no information that's available to one player but hidden from the other, which is the definition for perfect information. On a theoretical level, what makes it different from chess is the element of luck introduced by the dice. This makes it stochastic.

For many games, it's impossible to evaluate every possible outcome in order to find the best move. Instead, we use an n-move look-ahead strategy (where a move is often called a ply). [6, pp. 73&78] For this reason, there are basically two classes of algorithms that we need. The first generates sets of game states that we are likely to see in the future, and the second makes educated guesses about a given board when we don't have time to wait for a definite answer.

We'll now give an overview of six algorithms:

- Minimax Using a tree structure to find the optimal strategy for games with perfect information.
- Expectimax Adding support for stochastic games to the game tree.
- Alpha-beta pruning Removing branches that seem unfruitful.
- *-Minimax Improving alpha-beta by also pruning chance nodes.
- Knowledge-based Evaluation based on rules dictated by an expert.
- Neural networks Evaluation based on a neural network that has been exposed to thousands of games.

4.1 **Minimax**

For evaluating non-stochastic games, we can assume that both players play rationally. We define rational as in every game state choosing a move that guarantees victory, if there is one, which is equivalent to limiting the opponent's possibilities to make a good move as much as possible. In a twoplayer game, a given player who's ready to make a move (called MAX from here on) should pick a path if we don't care about the order of x and y.

that prevents the opponent (called MIN) from getting a chance to win. In that sense, MAX is always trying to choose the path that promises the maximum possible return, knowing that MIN is always trying to minimize it. [2][6, p. 74]

Given these simple rules, we can construct a game tree, with the leaves denoting a win (+1), a loss (-1) or a draw (0). As мах plays rationally, he treats a game state as winning if there's at least one path that'll make him win. Therefore, the value minimax(v) of an internal MAX node vis $\max_{u \in children(v)}$, and, similarly, the value of an internal MIN node v is $\min_{u \in \text{children}(v)}$.

4.2 Expectimax

Expectimax is a variant of Minimax, used for stochastic games, where weights are used to evaluate the likelihood of different scenarios. In a nonstochastic game, MAX and MIN would just have made alternating moves, which means that the Minimax tree consists of alternating MAX and MIN move nodes. The Expectimax tree, on the other hand, is constructed by placing chance nodes between every move node in the hierarchy. This is because after MAX has made his move, MIN rolls the dice before making his move and so on. When calculating the expected value of a move node, the probability of the chance children are taken into consideration. [6, p. 86]

In our case, the probability of a dice roll $\{x, y\}$ is given by

$$P(\{x, y\}) = \begin{cases} 1/36, & x = y \\ 1/18, & x \neq y \end{cases}$$

4.3 Alpha-beta pruning

The Expectimax tree quickly grows enormous. If we assume that every node has b children (the branching factor) and the depth of the tree is *d*, the complexity of the problem will be $O(b^d)$. [6, p. 78] The gameplay in backgammon, even in a situation where both players make random moves, tends to move towards an end state, as movement forward along the path is more common than being hit, placed on the bar and having to start over. It is, however, entirely possible to find sequences of movements that would result in an endless game (consider one checker from each player that always gets hit by the other when it has reached it's home board). Such a game is very unlikely, but it proves that the game tree can grow infinitely large. Thus, we need to find a way to limit the branches that we decide to explore.

One way to optimize the search, is to use Alphabeta pruning. Assume that MAX is about to make his move, and that he has several options to choose from. He knows that MIN will choose the minimal score he can find among his options. This means that if we notice that one of the children of the MIN node offers a value equal to or worse than a MIN node we have already seen, we can immediately stop evaluating those children, as MAX knows that choosing that option would give MIN a better game state than necessary, and it can never help us to continue with that node. In the same way, we can stop evaluating children to a MAX node that are equal to or better than a MAX node that we have already seen. [6, p. 82]

The algorithm makes use of this fact by assigning an α -value to the MAX node, a value that can never decrease. Once MAX has seen a particular α , he knows that it is the lowest possible value he can expect and will not consider anything worse. In the same way, a MIN node is associated with a β -value, which can never increase. As soon as these conditions are broken, we prune beneath the node and continue on to the next.

4.4 *-Minimax

Improvements to Alpha-beta pruning were suggested already in 1983, but they didn't receive much attention until recently, and they aren't used much. The Star1 algorithm makes use of the fact that we can prune the children of a chance node as well, since we know the probability and the upper and lower limits of the value function. The further improved Star2 requires that a chance node is followed by a MAX/MIN-node, and does a preliminary probing that might improve the efficiency of the search. If it fails, the program can still continue as Star1. [2][8]

4.5 Knowledge-based evaluation

Knowledge-based algorithms were common in the early backgammon programs, mostly because of the limited computational power. In 1979, a knowledge-based program called *BKG* defeated the world champion Luigi Villa 7–1. However, the author later admitted that the program had been lucky with the rolls, and probably wouldn't have won otherwise. [2]

4.6 Neural networks

The most successful backgammon programs today use artificial neural networks to evaluate specific game states. *Neurogammon*, constructed by Gerald Tesauro, was an early example using an artificial neural network, trained through supervised learning. In other words, a human was feeding it game states and told it which the correct outcome should be. Tesauro went on to creating *TD-Gammon*, which learned backgammon through self-play. Since backgammon is a stochastic game, it could avoid ending up in, and thus only learning about, a specific local area because of suboptimal training. TD-Gammon belongs to the top-3 players in the world. [2][4, pp. 210–212][7]

Another excellent backgammon program using artifical neural networks is the freely distributed *GNU Backgammon*, which outperforms commercial competitors. Apart from forward pruning as a means of reducing the number of game states, it also uses different neural networks depending on the situation, it contains an endgame database and so on. [2]

5 Constructing our own evaluation function

5.1 Research process

We started off by studying books, reports and lecture notes about Expectimax and Alpha-beta pruning in general, and backgammon AI in particular, to get an overall view of the current research. Then, we decided on a few basic strategies to evaluate, and constructed a rule engine creating a tree of possible moves and implemented the algorithms necessary to pick a path through the tree. This was done in C[#]. Finally, using tweaks to the algorithm, a small range of AI players with different tactics were then used to play a large number of games against each other. We were especially interested in finding out whether there was potentially one dominant player, or whether certain tactics are better suited when playing against opponents with certain other tactics.

5.2 Choice of game rules

Backgammon seemed to be an interesting game, because of the relatively simple set of rules (as opposed to chess, for example) and the natural flow of the game towards an end even when picking randomized legal moves (also as opposed to chess, as it happens). In other words, a rather naïve player would still without question be able to play the game to the end, although maybe not at a very proficient level.

One thing that troubled us with the classic backgammon rules was the doubling die, as it would require a secondary evaluation function to decide whether a game state seemed hopeless or, on the contrary, promising enough to raise the stakes. This secondary evaluation function would carry the risk of taking over the game, never allowing the primary evaluation function to play all the way to the end.

Knowing about the Greek versions of the game, we instead decided to focus on the game of Portes. While it has the element of a double win in case all of the winner's checkers are borne off before any of the opponent's are, that has little effect on the gameplay. For human players, this rule makes the game interesting even after it's become obvious who'll win, but a computer is not affected by those feelings. Still, there might be a tendency to take higher risks when there's nothing more to lose, but we believe that the effect on the gameplay would be minor and difficult to take into account.

Having decided on Portes, we wanted to mention Fevga and Plakoto as well, since they are usually played one after each other. We discussed implementing rule engines for them too, but that would've made it more difficult to reach a conclusion. Our suggestions regarding the other games are mentioned in section 8.

5.3 Choice of algorithm

Most modern backgammon programs use Expectimax in some form. [2][5] The theory behind it is also perfectly sound, which made it more or less mandatory for us to implement our software using these algorithms. Our aim, however, was to have a look at evaluation functions that differ from the most common ones.

Given that artificial neural networks are complicated, take a lot of time and resources to train, and the result of the algorithmic fine-tuning of the layers is almost impossible to understand, let alone motivate in an academic paper, we decided to settle for knowledge-based algorithms. Implementing an artificial neural network may very well be a nice exercise in artificial intelligence, but it might not deliver many new insights to a project. Most of all, it's extremely difficult to explain why the neural network behaves in a certain way. By instead focusing on creating knowledge-based players, we could draw conclusions about which primitive evaluation functions seem to work well in a lookahead environment.

Last but not least, we also discussed what a human player is really looking for. There are already backgammon programs out there that could beat the world champions. Maybe what the world needs is not another one that is exactly the same, but rather an opponent that a human player can learn to master?

5.4 Rule engine

The rule engine in our system is fed a game state, a dice roll and which of the players is about to move. It is supposed to return a list of new games states that are possible given this information. What we have to keep in mind, is that a set of dice $\{x, y\}$,

where $x \neq y$, can yield different results depending on the order we choose to make the moves. Consider the state depicted in Figure 4, where Black is about to move. If he gets the dice roll {1,2}, he can choose to move 1–2–4 or 1–3–4, since he decides which move to play first. The final position of the Black checker will be the same, but landing on point 2 will hit White's blot on the way.

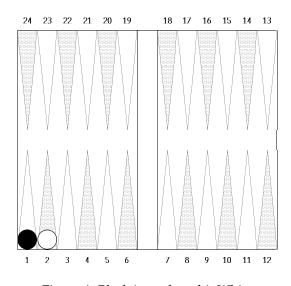


Figure 4: Black is ready to hit White

While this might sound tricky, the implementation is rather straight-forward. The first step is to create a function that returns all game states that are possible after moving a single checker. This function tries to move a checker from the bar, if there is one there. Otherwise, it tries to move a checker from every occupied point on the board. There are five possibilities:

- The checker can be moved to either an empty point, or to a point occupied by checkers of the same color.
- 2. The checker hits a blot of the opposite color, and remains at that point. The blot is moved

to the bar.

- The checker can be borne off, if it can be done with the exact number of steps to leave the board, but only if all checkers are in the home board.
- 4. The checker can be borne off, if it can be moved at least the necessary number of steps and it's standing on the rearmost occupied point along the path.
- 5. The checker cannot be moved.

Having coded this function, the rest is just a matter of using the function sequentially to try all possibilities of the dice roll in any order, and for the special case that the dice show the same numbers, instead running the function sequentially four times. If it turns out that an empty list is returned at any stage (indicating no possible moves), we settle for the last non-empty list. Any duplicated state is of course important to remove to increase efficiency.

Since the rule engine is such an important part of the solution, we decided to independently design our own rule engines. We then tested them on the same input data, to make sure that the output was exactly the same. Once we were certain that the programs produced the same sets of possible moves, one of them was discarded. The reason for spending extra time with the rule engine was that an AI player can be more or less clever in the way it makes its decisions, but as long as the rule engine is guaranteed to be correct, the AI players are forced to obey the rules of the game. In other words, with a buggy rule engine, none of the results of the test runs could be used to draw conclusions, whereas a buggy player could only affect its own results. What's more, the distinction between bugs

and poor performance is a bit more fuzzy for an AI player.

5.5 Al players

We constructed several evaluation functions, and discussed which properties should be tested. We agreed that most of the strategic game states that we could come up with should be possible to detect without explicitly trying to make forecasts to find them. For example, struggling to place the checkers so that they are in reach of hitting the opponent's blots might be meaningless, since the game tree should be able to find these opportunities automatically through the lookahead. Contrarily, the more sophisticated the algorithm tries to be, the more prone it is to exhibit unintended side effects. Besides, if we actually managed to construct an AI player that predicts the future successfully for a given board, it also gets an unfair advantage to other algorithms as it would be similar to evaluating the game tree to different levels for different algorithms. Thus, we decided that only the most basic properties should be tested.

We are in no way experts on backgammon, and hence based the strategy on what is well-known about the game. Since the overall strategy of Portes is to build doors, we decided to base one strategy on building many doors (in the ideal case as many doors with two checkers as possible) and another on avoiding being hit (which means that we don't care about the number of doors). We wanted to limit the scores for all evaluation functions to the interval [-1, 1], partly to make them easier to understand for a human, and partly to make certain that we won't accidentally overflow a variable or lose precision. The output from the evaluation functions doesn't have to be comparable between the different functions, though, as they are only measured against themselves for different game states. After having experimented we settled on these players:

Hit₁ Prefers hitting the opponent's blots. This is done by calculating the evaluation scores

$$e(s, \text{max}) = .055 \times h_{\text{min}}$$
 and
 $e(s', \text{min}) = -.055 \times h'_{\text{max}}$

for the game states *s* and *s'* where h_{MIN} and h'_{MAX} are the number of the opponent's checkers currently placed on the bar (i.e. waiting to be entered into the board) in their respective game states. Since there are only 15 checkers, we get $e(s, \text{MAX}) \in [0, .825]$. As we can see, the score is proportional to the number of checkers on the bar, which means that a game state where we would hit one checker with 100 % probability is considered equivalent to a game state where we would hit two checkers with 50 % probability and none with 50 %.

Hit₂ Tries to hit the opponent's blots, while protecting its own. It using proportional scores like Hit₁, but focuses on the difference in checkers on the bar between the opponent and itself,

$$e(s, \text{MAX}) = .055 \times (h_{\text{MIN}} - h_{\text{MAX}})$$
 and
 $e(s', \text{MIN}) = -.055 \times (h'_{\text{MAX}} - h'_{\text{MIN}}).$

In this case, $e \in [-.825, .825]$.

Door Prefers building many doors and limiting the same for the opponent, by assigning a score proportional to the difference in number of doors,

$$e(s, \text{MAX}) = .05 \times (d_{\text{MAX}} - d_{\text{MIN}})$$
 and
 $e(s', \text{MIN}) = -.05 \times (d'_{\text{MIN}} - d'_{\text{MAX}}),$

where d_{MAX} and d_{MIN} represent the number of points with at least two of the respective player's own checkers. With 15 checkers, there can be a maximum of 7 doors, and we get $e \in [-.35, .35]$. Note that this strategy is not the same as avoiding blots. Such a strategy would not care whether the doors have many checkers on them or only a few, as long as we're not leaving any checkers alone.

DoorHit¹ With this player, we started experimenting for real. This one wants to hit the opponent's blots while protecting its own. At the same time, it prefers doors. Using the same notation as above, this is the player we settled for:

$$e(s, \text{MAX}) = .025 \times (d_{\text{MAX}} - d_{\text{MIN}}) + .02525 \times (h_{\text{MIN}} - h_{\text{MAX}}) \text{ and}$$
$$e(s', \text{MIN}) = -.025 \times (d'_{\text{MIN}} - d'_{\text{MAX}}) - .02525 \times (h'_{\text{MAX}} - h'_{\text{MIN}})$$

The result is $e \in [-.55375, .55375]$.

DoorHit₂ Similar to **DoorHit**₁ but with more complicated calculations. Hits the opponent's blots, protects its own, prefers doors (small ones) with increasing value if the doors are placed in the home board. From the perspective of player MAX, a door *i* is assigned a cumulative grade

$$n_i = \begin{cases} 2, & \text{for a door of MAX checkers} \\ +1, & \text{iff in MAX's home board} \\ -1, & \text{iff more than 4 checkers} \end{cases}$$

For the opponent's doors, another cumulative grade is calculated for each door *j*:

 $m_j = \begin{cases} -2, & \text{for a door of MIN checkers} \\ +1, & \text{iff more than 4 checkers} \end{cases}$

These grades are then combined with the number of checkers on the bar:

$$e(s, \text{max}) = .01 \times \left(\sum_{i} n_{i} + \sum_{j} m_{j}\right) + .029 \times (h_{\text{min}} - h_{\text{max}})$$

e(s', MIN) is calculated similarly. For this evaluation function, $e \in [-.635, .635]$.

Random Completely random moves, for comparison. The score is calculated uniformly so that

$$e \in [-1, 1].$$

The idea with these players was that they'd return a constant reward or penalty based on a count of hits or doors. They are really primitive, but they are mostly meant to be simple enough so that their behavior can be compared and understood.

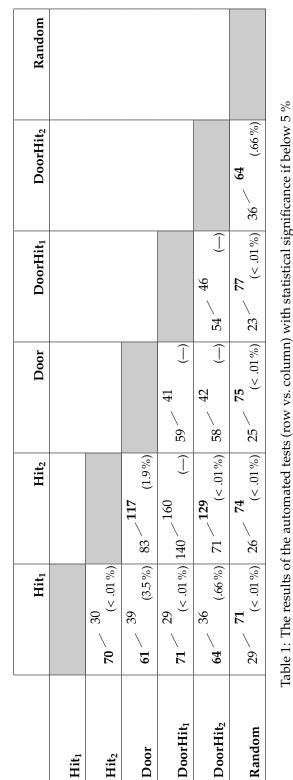
We also tried to implement a player that valued states that gave him a lot of options, since a very limited set of options generally means that the opponent has an advantage in some way. Unfortunately, it turned out that the calculation of how many possible moves there are was too expensive to try out, even when reducing the depth of the tree.

5.6 Automated test framework

We constructed an automated test harness in order to let the different players compete against each other. It didn't try to modify or develop the players itself, but rather simplified the execution of the programs, while keeping track of the scores.

6 Results

Using Expectimax with Alpha-beta pruning and a depth (ply) of 3, we tested all combination of our



six players against each other. These tests were generally performed in series of 100 games, but we ran more games with a few of them, to get more reliable results. The outcome of these tests can be viewed in Table 1. For each result, we ran a twotailed sign test. We decided on a cut-off for our presentation of *p*-values at 5 %. Anything above that should be run a substantial number of times more if we want to reach any conclusions.

First, we noted that the player **Random** loses to all other players. This means that our AI players are working, as they are at least doing a better job than pure randomness does. While we have to admit that it was a bit discouraging that they didn't perform even better, we have to keep in mind that they all use extremely basic strategies. Even though there might be theoretical discussions about the usage for a randomizing player, we had no longer any need for it for the purpose of developing an evaluation function, and could therefore discard it.

Having removed Random, we could clearly see that Hit₁ was losing to all the remaining players. Among the rest, however, the patterns are not completely obvious. Of course, Hit₂ performed well against Door as well as against DoorHit2, but DoorHit₁ put up a good fight. Actually, when just looking at the numbers, it seems like a cycle is almost formed as Hit₂ is better than DoorHit₂, which is slightly better than **DoorHit**₁, which is virtually as good as Hit₂. This reminds us of games like rock-paper-scissors, where there is no absolute winner but rather different ways of beating different opponents. In our case, though, we concluded that Hit₂ outperformed all other players except for one, which it still performed well against. Thus, we declared Hit₂ the winner.

7 Conclusions

The tests took a long time to run, and if we had had the computational power to run more of them we could've received results that were statistically better. However, we believe that it wouldn't have changed anything.

Hit₂ was the player that tried to hit the opponent's blots while protecting its own. We find it facinating that such a simple set of rules can prove to be the dominant one, but are at the same time surprised that the very similar Hit₁ performed so poorly. It seems that halfway right can be completely wrong. But the explanation for the success of Hit₂ might be that it turned out to be a good strategy for building doors as well (since it dislikes lonely checkers), while the purely door-building player might not have been able to pose a threat to the opponent, or even maintain an offensive position on its own in the long run if it at the same time wanted to maximize the number of doors.

We have managed to construct a player that outperforms several other players, and especially a random player. We do realize, however, that a human player would likely easily defeat it. The program might perhaps be able to play against novice human players, but it's not difficult to understand why modern backgammon programs are based on artificial neural networks.

8 Further research

A possible continuation of this work, might be to develop the test framework into one that automatically runs tests for a long time while genetically mutating different variables, and maybe also using different evaluation functions with variable weights. At the same time, tests against a human player would be interesting, to see to which level [7] Tesauro, G. 1995, 'Temporal Difference Learnthis program could evolve. [7] ing and TD-Gammon', *Communications of the*

Another interesting topic is whether similar strategies would work for the other games, explained in section 3, if the players are used together with different rule engines. What are the common denominators for these games?

9 Acknowledgements

We'd like to thank Andreas Giallourakis for spending time teaching us the game.

References

- [1] Backgammon Galore, http://www.bkgm.com/ [viewed 2011-04-14]
- [2] Hauk, T., Buro, M. & Schaeffer, J. 2004, '*-Minimax Performance in Backgammon', Proceedings of Computers and Games, pp. 51– 66, available online: http://skatgame.net/ mburo/ps/STAR-B.pdf [viewed 2011-04-14]
- [3] Kalai, G. 2011, Is Backgammon in P?, blog entry, http://gilkalai.wordpress.com/2011/ 01/14/is-backgammon-in-p/
- [4] Nilsson, N. 1998, Artificial Intelligence: A New Synthesis, Morgan Kaufmann, San Francisco, USA
- [5] Scott, J. 2001 The Neural Net Backgammon Programs, available online: http://satirist. org/learn-game/systems/gammon/ [viewed 2011-04-14]
- [6] Smed, J. & Hakonen, H. 2006, Algorithms and Networks for Computer Games, John Wiley & Sons, Ltd, West Sussex, England

- 7] Tesauro, G. 1995, 'Temporal Difference Learning and TD-Gammon', *Communications of the ACM*, vol. 38, no. 3, March 1995, available online: http://www.research.ibm.com/ massive/tdl.html [viewed 2011-04-14]
- [8] Veness, J. 2006, Expectimax Enhancements for Stochastic Game Players, Bachelor thesis, The University of New South Wales School of Computer Science and Engineering, available online: http://jveness.info/publications/ thesis.pdf [viewed 2011-04-14]